

# introduction

---

## Sergiy Pereverzyev

PhD student at  
Fraunhofer Institut  
Techno- und  
Wirtschaftsmathematik,  
Department Transport Processes,  
Kaiserslautern, Germany



**Fraunhofer** Institut  
Techno- und  
Wirtschaftsmathematik

# introduction

---

## Sergiy Pereverzyev

PhD student at

Fraunhofer Institut

Techno- und

Wirtschaftsmathematik,

Department Transport Processes,

Kaiserslautern, Germany

Sci.supervisors:

Prof. H.Neunzert

Prof. R.Pinnau

Dr. N.Siedow



**Fraunhofer**

Institut  
Techno- und  
Wirtschaftsmathematik

# introduction

---

## Sergiy Pereverzyev

PhD student at

Fraunhofer Institut

Techno- und

Wirtschaftsmathematik,

Department Transport Processes,

Kaiserslautern, Germany

Sci.supervisors:

Prof. H.Neunzert

Prof. R.Pinnau

Dr. N.Siedow

Sci.interests:

regularization

of inverse problems



**Fraunhofer**

Institut  
Techno- und  
Wirtschaftsmathematik

# regularized fixed-point

---

$$\hat{u}: \quad Fu = y$$



**Fraunhofer** Institut  
Techno- und  
Wirtschaftsmathematik

# regularized fixed-point

---

$$\hat{u}: \quad Fu = y \quad F = A + G$$



# regularized fixed-point

---

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$Au = y - Gu$$



# regularized fixed-point

---

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$Au_{k+1} = y - Gu_k$$



# regularized fixed-point

---

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$Au_{k+1} = y_\delta - Gu_k$$





# regularized fixed-point

---

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$A^* Au_{k+1} = A^*(y - Gu_k)$$



# regularized fixed-point

---

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$u_{k+1} = (A^*A)^\dagger A^*(y - Gu_k)$$



# regularized fixed-point

---

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$u_{k+1} = (A^* A)^\dagger A^* (y - Gu_k)$$

$$u_{k+1}^\alpha = g_\alpha (A^* A) A^* (y_\delta - Gu_k)$$



# regularized fixed-point

---

$$\hat{u}: \quad Fu = y \quad F = A + G$$

$$u_{k+1} = (A^*A)^\dagger A^*(y - Gu_k)$$

$$u_{k+1}^\alpha = g_\alpha(A^*A)A^*(y_\delta - Gu_k)$$

$$\|\hat{u} - u_{k+1}^\alpha\| \leq \varphi(\alpha) + \frac{\delta}{\lambda(\alpha)} + \rho\|\hat{u} - u_k\|$$



# balancing principle

---

$$\|\hat{u} - u^\alpha\| \leq \varphi(\alpha) + \frac{\delta}{\lambda(\alpha)}$$

$$\Delta = \{\alpha_i, i = 1, \dots, N\}$$



# balancing principle

---

$$\|\hat{u} - u^\alpha\| \leq \varphi(\alpha) + \frac{\delta}{\lambda(\alpha)}$$

$$\Delta = \{\alpha_i, i = 1, \dots, N\}$$

$$i_{\text{opt}} = \max \left\{ i \mid \|u^{\alpha_i} - u^{\alpha_j}\| \leq \frac{4\delta}{\lambda(\alpha_j)}, j = 1, \dots, (i-1) \right\}$$



# balancing principle

---

$$\|\hat{u} - u^\alpha\| \leq \varphi(\alpha) + \frac{\delta}{\lambda(\alpha)}$$

$$\Delta = \{\alpha_i, i = 1, \dots, N\}$$

$$i_{\text{opt}} = \max \left\{ i \mid \|u^{\alpha_i} - u^{\alpha_j}\| \leq \frac{4\delta}{\lambda(\alpha_j)}, j = 1, \dots, (i-1) \right\}$$

$$\|\hat{u} - u^{\alpha_{i_{\text{opt}}}}\| \leq b(\delta)$$



# balancing principle

---

$$\|\hat{u} - u^\alpha\| \leq \varphi(\alpha) + \frac{\delta}{\lambda(\alpha)}$$

$$\Delta = \{\alpha_i, i = 1, \dots, N\}$$

$$i_{\text{opt}} = \max \left\{ i \mid \|u^{\alpha_i} - u^{\alpha_j}\| \leq \kappa \frac{4\delta}{\lambda(\alpha_j)}, j = 1, \dots, (i-1) \right\}$$

$$\|\hat{u} - u^{\alpha_{i_{\text{opt}}}}\| \leq b(\delta)$$





# balancing principle

---

$$\|\hat{u} - u^\alpha\| \leq \varphi(\alpha) + \frac{\delta}{\lambda(\alpha)}$$

$$\Delta = \{\alpha_i, i = 1, \dots, N\}$$

$$i_{\text{opt}} = \max \left\{ i \mid \|u^{\alpha_i} - u^{\alpha_j}\| \leq \kappa \frac{4\delta}{\lambda(\alpha_j)}, j = 1, \dots, (i-1) \right\}$$

$$\|\hat{u} - u^{\alpha_{i_{\text{opt}}}}\| \leq b(\delta)$$

Hui Cao

RICAM,

Group Inverse Problems



Fraunhofer

Institut  
Techno- und  
Wirtschaftsmathematik